

Hodnoty goniometrických integrálů:

$$\int_0^{\pi/2} \cos^m(x) \sin^n(x) dx = \frac{\Gamma\left(\frac{m+1}{2}\right)\Gamma\left(\frac{n+1}{2}\right)}{2 \cdot \Gamma\left(\frac{m+n+2}{2}\right)}; \quad \Gamma(n) = (n-1)!; \quad \Gamma\left(n + \frac{1}{2}\right) = \sqrt{\pi} \frac{(2n-1)!!}{2^n}$$

Hodnoty jacobíánů vybraných souřadnic:

$$\begin{aligned} x &= s + a\rho \cos(\varphi) \\ y &= t + b\rho \sin(\varphi) \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y)}{\mathcal{D}(\rho, \varphi)} \right) = ab\rho.$$

$$\begin{aligned} x &= s + a\rho \cos^\alpha(\varphi) \\ y &= t + b\rho \sin^\alpha(\varphi) \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y)}{\mathcal{D}(\rho, \varphi)} \right) = ab\alpha\rho \cos^{\alpha-1}(\varphi) \sin^{\alpha-1}(\varphi).$$

$$\begin{aligned} x &= s + a\rho \cos(\varphi) \\ y &= t + b\rho \sin(\varphi) \\ z &= u + c h \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y, z)}{\mathcal{D}(\rho, \varphi, h)} \right) = abc\rho.$$

$$\begin{aligned} x &= s + a\rho \cos^\alpha(\varphi) \\ y &= t + b\rho \sin^\alpha(\varphi) \\ z &= u + c h \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y, z)}{\mathcal{D}(\rho, \varphi, h)} \right) = abca\rho \cos^{\alpha-1}(\varphi) \sin^{\alpha-1}(\varphi).$$

$$\begin{aligned} x &= s + a\rho \cos(\vartheta) \cos(\varphi) \\ y &= t + b\rho \cos(\vartheta) \sin(\varphi) \\ z &= u + c\rho \sin(\vartheta) \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y, z)}{\mathcal{D}(\rho, \varphi, \vartheta)} \right) = abc\rho^2 \cos(\vartheta).$$

$$\begin{aligned} x &= s + a\rho \cos^\beta(\vartheta) \cos^\alpha(\varphi) \\ y &= t + b\rho \cos^\beta(\vartheta) \sin^\alpha(\varphi) \\ z &= u + c\rho \sin^\beta(\vartheta) \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y, z)}{\mathcal{D}(\rho, \varphi, \vartheta)} \right) = \\ = abca\beta\rho^2 \cos^{2\beta-1}(\vartheta) \sin^{\beta-1}(\vartheta) \cos^{\alpha-1}(\varphi) \sin^{\alpha-1}(\varphi).$$

$$\begin{aligned} x &= s + a\rho \cos(\omega) \cos(\vartheta) \cos(\varphi) \\ y &= t + b\rho \cos(\omega) \cos(\vartheta) \sin(\varphi) \\ z &= u + c\rho \cos(\omega) \sin(\vartheta) \\ w &= v + d\rho \sin(\omega), \end{aligned} \quad \det \left(\frac{\mathcal{D}(x, y, z, w)}{\mathcal{D}(\rho, \omega, \varphi, \vartheta)} \right) = abcd\rho^3 \cos^2(\omega) \cos(\vartheta).$$